Recall: A basis of vector space V is any subset BEV Such that OB is lin. ind. @ B spans V. "The only lin comb. giving Ov * is the Zero-combinations" "Every vector in V is a linear comb. of vectors from B" Prop: B is a bacis of V iff every vector of V arises as a unique lin. Lond of elts from B. Recall: dim (V) = number of elements in a basis for V. Exi R" has dimension ni En= {e,,ez;...,n}. Recall: L: V-sW is linear when for all u,v & V and all CEIR we have $L(u+c\cdot v) = L(u)+c\cdot L(v)$.

NB: easiest condition to check... The rank of L is dim (ran (L)).
The nullity of L is dim (ker (L)). range of L is ran(L) = { L(v) : v ∈ V} Lyie. Set of outputs of function L Kernel of L is ker(L) = \{v \in V: L(v) = Ow}\}
Lie set of vectors mapping to Ov under L. Rank-Nullity Formula: dim (dan(L)) = rank(L) + nullify(L). Ex: D= {(i),(i),(i)}. Show D is dependent. Method: a(i) + b(i) + c(i) = (i)

$$= \{(a-c)V_1 + (b+c)V_2 : a,b,c \in \mathbb{R}\}$$

$$= \{(aV_1 + \beta V_2 : x, p \in \mathbb{R}\}\}$$

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$$\frac{Sol}{x} \times \begin{pmatrix} 1 & 0 \\ 0 & 1 \end{pmatrix} + y \begin{pmatrix} 1 & 1 \\ 0 & 0 \end{pmatrix} + z \begin{pmatrix} 0 & 1 \\ 1 & 0 \end{pmatrix} + w \begin{pmatrix} 0 & 0 \\ 1 & 1 \end{pmatrix} = \begin{pmatrix} 0 & 0 \\ 0 & 0 \end{pmatrix}$$

iff
$$(x+y)$$
 $y+z$ = $(x+y)$ = $(x+y$

To compte a besis for range: $ran(L) \stackrel{*}{=} \left\{ L(v) : v \in dom(L) \right\}$ $\stackrel{*}{=} \left\{ L(a + bx + cx^2 + dx^3) : a,b,c,d \in \mathbb{R} \right\}$